

Unit 5 Formulas/Info you can use on the test

Hypothesis Tests:

- State Hypotheses (in symbols and in words)
- Check conditions (SRS, independence, $n < 10\% \text{pop}$, $np, nq \geq 10$)
- Compute p-value (state what test in calculator, show what was entered, report Z and p-value)
- Conclusion (example): With significance of .05, p-value=0.02 is low so we reject H_0 .
We do have sufficient statistical evidence to conclude (H_a).

Explaining p-value: If 78% of DV seniors were actually still staying in state for college, our p-value of .09 means there is a 9% probability of this sample's result (85% staying in state) or higher occurring just due to chance.

Confidence Intervals:

- Check conditions (SRS, independence, $n < 10\% \text{pop}$, $np, nq \geq 10$)
- Compute the confidence interval (state which function in calculator, show what was entered, report the resulting interval).
- Conclusion (example): We are 90% confident that the true difference in percentage of students staying in state for college (this year – last year) is between 2.4% and 3.8%.

Explaining confidence level: If we were to take many samples of size 40 and compute confidence intervals for each, 90% of the confidence intervals would contain the true percentage of all DV seniors who are staying in state this year.

Errors:

Null Hypothesis is:

		True	False
Decision:	Reject	Type I Error α	OK (power) $1 - \beta$
	Not Reject	OK	Type II Error β

$$P(I) = \alpha$$

$$P(II) = \beta$$

$$\text{Power of the Test} = 1 - \beta$$

Things that increase Power:

- (for fixed n): Increasing α : $\alpha \nearrow$, $\beta \searrow$, Power \nearrow
- Increasing n: $n \nearrow$, $\alpha \searrow$, $\beta \searrow$, Power \nearrow
- Larger Effect Size

Sample Size Calculations:

margin of error

$$CI = \hat{p} \pm z^* \sqrt{\frac{\hat{p}\hat{q}}{n}} \quad \text{so...} \quad z^* \sqrt{\frac{\hat{p}\hat{q}}{n}} = \text{required margin of error}$$

(use $\hat{p} = 0.5$ and round n up to guarantee the margin of error)

Common z^* values: 90%: $z^*=1.64$, 95%: $z^*=1.96$, 99%: $z^*=2.576$

Sampling distributions for proportions:

Random Variable	Parameters of Sampling Distribution	Standard Error* of Sample Statistic
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For one population:

\hat{p}	$\mu_{\hat{p}} = p$	$\sigma_{\hat{p}} = \sqrt{\frac{p(1-p)}{n}}$	$s_{\hat{p}} = \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$
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For two populations:

$\hat{p}_1 - \hat{p}_2$	$\mu_{\hat{p}_1 - \hat{p}_2} = p_1 - p_2$	$s_{\hat{p}_1 - \hat{p}_2} = \sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}}$	
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When $p_1 = p_2$ is assumed :

$\sigma_{\hat{p}_1 - \hat{p}_2} = \sqrt{\frac{p_1(1-p_1)}{n_1} + \frac{p_2(1-p_2)}{n_2}}$	$s_{\hat{p}_1 - \hat{p}_2} = \sqrt{\hat{p}_c(1-\hat{p}_c)\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}$
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where $\hat{p}_c = \frac{X_1 + X_2}{n_1 + n_2}$

Sampling distributions for means:

Random Variable	Parameters of Sampling Distribution	Standard Error* of Sample Statistic
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For one population:

\bar{X}	$\mu_{\bar{X}} = \mu$	$\sigma_{\bar{X}} = \frac{\sigma}{\sqrt{n}}$	$s_{\bar{X}} = \frac{s}{\sqrt{n}}$
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For two populations:

$\bar{X}_1 - \bar{X}_2$	$\mu_{\bar{X}_1 - \bar{X}_2} = \mu_1 - \mu_2$	$\sigma_{\bar{X}_1 - \bar{X}_2} = \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}$	$s_{\bar{X}_1 - \bar{X}_2} = \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$
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