

**14. Quality control.** Production managers on an assembly line must monitor the output to be sure that the level of defective products remains small. They periodically inspect a random sample of the items produced. If they find a significant increase in the proportion of items that must be rejected, they will halt the assembly process until the problem can be identified and repaired.

$H_0$ : assembly process is ok  
(acceptable level of defects)

$H_a$ : assembly process is broken  
(defects too high)

		$H_0$	$H_a$
R	I	F	
NF		I	F

- In this context, what is a Type I error?
- In this context, what is a Type II error?
- Which type of error would the factory owner consider more serious?
- Which type of error might customers consider more serious?

- Type I error means process is actually ok, but we think it's broken, so we stop production.
- Type II error means process is actually broken, but we think it's ok, don't stop, and ship bad product.
- Both are bad - type I means we lose money, type II means have to recall product
- type II error more serious (increased chance of getting defective product).

**16. Production.** Consider again the task of the quality control inspectors in Exercise 14.

- In this context, what is meant by the power of the test the inspectors conduct?
- They are currently testing 5 items each hour. Someone has proposed they test 10 each hour instead. What are the advantages and disadvantages of such a change?
- Their test currently uses a 5% level of significance. What are the advantages and disadvantages of changing to an alpha level of 1%?
- Suppose that as a day passes one of the machines on the assembly line produces more and more items that are defective. How will this affect the power of the test?

- power is the probability of correctly detecting the process is broken, if it is broken.
- higher  $n$ : Advantages: probability of type I and type II errors decreased, and power of test increased.

Disadvantages: more time consuming, using up more product in test.

- lower  $\alpha$ : Advantages: probability of type I error is decreased (less chance of stopping production unnecessarily). Also, increase power of test.  
Disadvantages: probability of type II error is increased (shipping bad product).
- effect size is increasing — this will increase the power of the test.

12. Alzheimer's. Testing for Alzheimer's disease can be a long and expensive process, consisting of lengthy tests and medical diagnosis. Recently, a group of researchers (Solomon *et al.*, 1998) devised a 7-minute test to serve as a quick screen for the disease for use in the general population of senior citizens. A patient who tested positive would then go through the more expensive battery of tests and medical diagnosis. The authors reported a false positive rate of 4% and a false negative rate of 8%.

	$H_0$	
	T	F
R	I	
N		II

- Put this in the context of a hypothesis test. What are the null and alternative hypotheses?
- What would a Type I error mean?
- What would a Type II error mean?
- Which is worse here, a Type I or Type II error? Explain.
- What is the power of this test?

a)  $H_0$ : patient does not have Alzheimer's

$H_a$ : patient has Alzheimer's

b) Type I error means  $H_0$  is true (patient does not have Alzheimer's) but we decide that they do (a false positive)

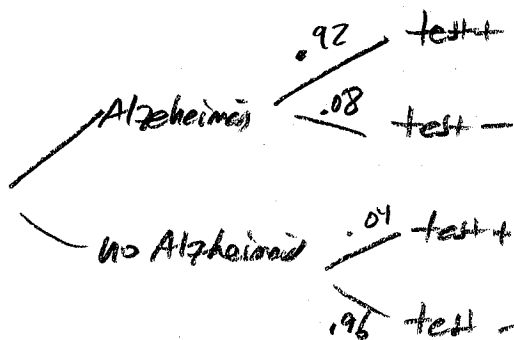
c) Type II error means  $H_0$  is false ( $H_a$  is true: patient does have Alzheimer's) but we decide they don't (false negative)

d) Consequences ... Type I: patient without Alzheimer's is diagnosed with Alzheimer's (and treated unnecessarily)

Type II: patient with Alzheimer's is not diagnosed (left untreated)

Type II is probably worse (although unnecessary medical treatment can also be bad).

e)



$$\text{power} = 1 - \beta = 1 - P(\text{Type II})$$

$$= 1 - P(\text{false negative})$$

$$= 1 - .08$$

$$= \boxed{.92}$$

If a patient has Alzheimer's there is a 92% chance this test will correctly detect it.

3. **Alpha.** A researcher developing scanners to search for hidden weapons at airports has concluded that a new device is significantly better than the current scanner. He made this decision based on a test using  $\alpha = 0.05$ . Would he have made the same decision at  $\alpha = 0.10$ ? How about  $\alpha = 0.01$ ? Explain.

If passed at  $\alpha = .05$ , would also pass at  $\alpha = .10$ ,  
but may or may not also be below  $\alpha = .01$   
(depends upon the actual  $\hat{p}$ , which we don't have)

5. **Significant?** Public health officials believe that 90% of children have been vaccinated against measles. A random survey of medical records at many schools across the country found that among more than 13,000 children only 89.4% had been vaccinated. A statistician would reject the 90% hypothesis with a P-value of  $P = 0.011$ .

- a) Explain what the P-value means in this context.  
b) The result is statistically significant, but is it important? Comment.
- a) If the true vaccination rate is 90%, there is a 1.1% chance that a sample of 13,000 children would find only 89.4% (or lower) vaccinated, just due to random chance.
- b) no. Although this result is statistically significant (due to the very large sample size) a 0.6% change is not practically significant.

**11. Homeowners.** In 2003 the Department of Commerce reported that 68.3% of American families owned their homes. In one small city, census data reveal that the ownership rate is much lower. The City Council is debating a plan to offer tax breaks to first-time home buyers in order to encourage people to become homeowners. They decide to adopt the plan on a 2-year trial basis and use the data they collect to make a decision about continuing the tax breaks. Since this plan costs the city tax revenues, they will continue to use it only if there is strong evidence that the rate of home ownership is increasing.

- In words, what will their hypotheses be?
- What would a Type I error be?
- What would a Type II error be?
- For each type of error, tell who would be harmed.
- What would the power of the test represent in this context?

e) The power to detect the an actually effective program is, in fact, effective.

a)  $H_0$ : no change in rates ( $p = .683$ )  
 $H_a$ : increase in rates ( $p > .683$ )

b) program is ineffective, but we detect an increase.  
 c) program is effective, but we fail to detect the increase.

d) Type I: taxpayers pay more for a program which doesn't work  
 Type II: potential home owners don't get assistance that would have worked.

**17. Equal opportunity?** A company is sued for job discrimination because only 19% of the newly hired candidates were minorities when 27% of all applicants were minorities. Is this strong evidence that the company's hiring practices are discriminatory?

- Is this a one-tailed or a two-tailed test? Why?
- In this context, what would a Type I error be?
- In this context, what would a Type II error be?
- In this context, describe what is meant by the power of the test.
- If the hypothesis is tested at the 5% level of significance instead of 1%, how will this affect the power of the test?
- The lawsuit is based on the hiring of 37 employees. Is the power of the test higher than, lower than, or the same as it would be if it were based on 87 hires?

a) one-tailed because we are interested only in why the % is low.

b)  $H_0$ : not discriminating ( $p = .27$ )  
 $H_a$ : discriminating ( $p < .27$ )

Type I would be detecting discrimination when company is not actually discriminating.

c) Type II would be failing to detect discriminating if company is actually discriminating.

d) Power = probability of detecting discrimination when it is actually occurring.

e)  $\alpha = .05$ ,  $1 - \beta = \text{power}$  will increase.

f) decreasing  $n$  would decrease the power.