

Verify the formula

$$1. \quad \frac{n \cdot 5^{n+2}}{5^{n+1}} = 5n$$

$$2. \quad \frac{(n+1) \cdot 4^n}{n \cdot 4^{n+1}} = \frac{n+1}{4n}$$

$$3. \quad \frac{(n+1)!}{(n-2)!} = (n+1)(n)(n-1)$$

$$4. \quad \frac{(2k-2)!}{(2k)!} = \frac{1}{(2k)(2k-1)}$$

Use the Ratio Test to determine the convergence or divergence of the series.

5.  $\sum_{n=1}^{\infty} \frac{1}{5^n}$

6.  $\sum_{n=1}^{\infty} \frac{1}{n!}$

7.  $\sum_{n=0}^{\infty} \frac{n!}{3^n}$

8.  $\sum_{n=1}^{\infty} \frac{6^n}{n!}$

9.  $\sum_{n=1}^{\infty} \frac{9^n}{n^5}$

10.  $\sum_{n=1}^{\infty} \frac{n}{4^n}$

11.  $\sum_{n=0}^{\infty} \frac{6^n}{(n+1)^n}$

12.  $\sum_{n=0}^{\infty} \frac{5^n}{2^{n+1}}$

$$13. \quad \sum_{n=1}^{\infty} \frac{(2n)!}{n^5}$$

$$14. \quad \sum_{n=0}^{\infty} \frac{(n!)^2}{(3n)!}$$

$$15. \quad \sum_{n=0}^{\infty} \frac{(-1)^n 2^{4n}}{(2n+1)!}$$

$$16. \quad \sum_{n=1}^{\infty} \frac{(-1)^n 3^n}{n 2^n}$$

Use the Root Test to determine the convergence or divergence of the series.

17.  $\sum_{n=1}^{\infty} \left(\frac{n}{2n+1}\right)^n$

18.  $\sum_{n=1}^{\infty} \left(\frac{2n}{n+1}\right)^n$

19.  $\sum_{n=2}^{\infty} \frac{(-1)^n}{(\ln(n))^n}$

20.  $\sum_{n=1}^{\infty} \left(-\frac{3n}{2n+1}\right)^n$

21.  $\sum_{n=1}^{\infty} (2\sqrt[n]{n} + 1)^n$

22.  $\sum_{n=0}^{\infty} e^{-3n}$

23.  $\sum_{n=1}^{\infty} \frac{n}{3^n}$

24.  $\sum_{n=1}^{\infty} \left(\frac{n}{500}\right)^n$

$$25. \quad \sum_{n=2}^{\infty} \frac{n}{(\ln(n))^n}$$

$$26. \quad \sum_{n=1}^{\infty} \frac{(n!)^n}{(n^n)^2}$$

Use either the Root Test or Ratio Test to determine the convergence or divergence of the series.

$$27. \quad \sum_{n=1}^{\infty} \frac{5 \cdot (-1)^{n+1}}{n}$$

$$28. \quad \sum_{n=1}^{\infty} \frac{100}{n}$$

29.  $\sum_{n=1}^{\infty} \frac{3}{n\sqrt{n}}$

30.  $\sum_{n=1}^{\infty} \left(\frac{2\pi}{3}\right)^n$

31.  $\sum_{n=1}^{\infty} \frac{5n}{2n-1}$

32.  $\sum_{n=1}^{\infty} \frac{n}{2n^2+1}$



Calculus 2 - Unit 10 Part 1 REVIEW

Determine whether the series diverges or converges.

You must show a valid test and work to justify your answer.

$$\#1) \sum_{n=1}^{\infty} \left( \frac{2n^3 + 1}{n^3 - 1} \right)^n$$

$$\#2) \sum_{n=1}^{\infty} \frac{8^n}{5^n}$$

$$\#3) \sum_{n=1}^{\infty} \frac{3^n}{4^n - 1}$$

$$\#4) \sum_{n=1}^{\infty} \frac{n}{\ln(n)}$$

$$\#5) \sum_{n=1}^{\infty} \frac{n!}{3^n}$$

$$\#6) \sum_{n=1}^{\infty} \frac{1}{5^n + 1}$$

$$\#7) \sum_{n=1}^{\infty} \frac{4n}{2n^2 + 1}$$

$$\#8) \sum_{n=1}^{\infty} \frac{2}{n^2}$$

$$\#9) \sum_{n=1}^{\infty} \frac{2n^3}{n^3 + 4}$$

$$\#10) \sum_{n=1}^{\infty} (-1)^n \frac{5n-1}{4n+1}$$

$$\#11) \sum_{n=0}^{\infty} 5 \frac{2^n}{3^n}$$

$$\#12) \sum_{n=1}^{\infty} \sin \left( \frac{(2n-1)\pi}{2} \right)$$

$$\#13) \sum_{n=1}^{\infty} \frac{1}{5^n}$$

$$\#14) \sum_{n=1}^{\infty} \frac{1}{2n-1}$$

$$\#15) \sum_{n=1}^{\infty} \frac{\ln(n)}{n^2}$$

$$\#16) \sum_{n=1}^{\infty} \frac{n}{n^2 + 1}$$

$$\#17) \sum_{n=1}^{\infty} (-2)^n$$

$$\#18) \sum_{n=1}^{\infty} \frac{5n^4}{n^4 + n^2 + 7}$$

$$\#19) \sum_{n=1}^{\infty} \frac{9^n}{n^5}$$

$$\#20) \sum_{n=1}^{\infty} \frac{5}{n^{0.4}}$$

$$\#21) \sum_{n=1}^{\infty} \left( \frac{n}{2n+1} \right)^n$$

$$\#22) \sum_{n=1}^{\infty} (-1)^n \frac{1}{3^n}$$

Determine whether the series converges absolutely, conditionally, or diverges:

$$\#23) \sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n!}$$

$$\#24) \sum_{n=1}^{\infty} (-1)^{n+1} \frac{1}{\sqrt{n}}$$

$$\#25) \sum_{n=1}^{\infty} (-1)^{n+1} \frac{n^2}{(n+1)^2}$$

#26) Determine the minimum number of terms required to approximate the sum of the series

$$\sum_{n=1}^{\infty} (-1)^{n+1} \frac{1}{2n^3 - 1} \text{ with an error of less than } 0.0005.$$