

Unit 1 Review (Precalculus topics) – **NO CALCULATORS**

Please show work so we can see how you find your solutions.

Function Notation and Composition of Functions:

#1. Let $f(x) = x - 2$ and $g(x) = x^3$. Find $g(f(4))$.

#2. Express the function $F(x) = \tan^3(x)$ in the form $f(g(x))$.

$$f(x) = \underline{\hspace{2cm}}$$

$$g(x) = \underline{\hspace{2cm}}$$

#3. If $f(x) = 2x^2 - 5x$, write $\frac{f(x+h) - f(x)}{h}$ in simplest form.

#4. Use the table to find the value of the function or composition at the given x .

x	-3	-1	0	3	5	7
$f(x)$	3	4	-1	-2	-1	5
$g(x)$	5	17	0	4	-3	-1

$$g(-1) = \underline{\hspace{2cm}}$$

$$f(g(5)) = \underline{\hspace{2cm}}$$

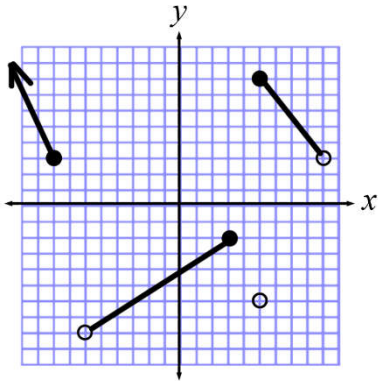
$$f(f(7)) = \underline{\hspace{2cm}}$$

#5. **Multiple Choice:** Relative to the graph $y = \cos x$, the graph of $y = 3\ln(x+2)$ is changed in what way?

- A) Shifted 2 units downward
- B) Compressed horizontally by a factor of 3
- C) Shifted 2 units to the right
- D) Stretched vertically by a factor of 3
- E) Shifted 2 units upward
- F) Shifted 2 units to the right and stretched 3 times vertically
- G) Shifted 2 units to the left and stretched 3 times vertically
- H) Shifted 2 units to the left

Domain/Range and Interval notation:

#6. State the domain and range of this function:



#7. **Multiple Choice:** The function $f(x) = \frac{x-2}{x-5} + \sqrt{(x-3)(x+2)}$ has as its domain all values of x such that

- A) $(-\infty, 2) \cup (2, 3) \cup (3, 5)$
- B) $[3, 5) \cup (5, \infty)$
- C) $(-\infty, 0) \cup [5, \infty)$
- D) $(-\infty, 0) \cup (3, 5) \cup (5, \infty)$
- E) $[3, 5]$
- F) $(3, 5) \cup (5, \infty)$
- G) $(-\infty, 0) \cup (5, \infty)$
- H) $(-\infty, 0) \cup [3, 5) \cup (5, \infty)$

#8. **Multiple Choice:** Let $f(x) = \sqrt{x+2}$ and $g(x) = \sqrt{x^2-9}$. Find the domain of $(fg)(x)$.

A) $(-\infty, -3) \cup (3, \infty)$

E) $(-\infty, -3] \cup [3, \infty)$

B) $(2, \infty)$

F) $[2, \infty)$

C) $(-\infty, -2)$

G) $(-\infty, -2]$

D) $[3, \infty)$

H) $(3, \infty)$

Factoring and Completing the Square:

#9. Factor completely: $x^2 + x - 42$

#10. Factor completely: $5x^2 - 13x + 6$

#11. Factor completely: $3x^4 - 48x^2$

#12. Complete the square to write the equation in the form of a circle: $x^2 + y^2 + 4x - 8y + 19 = 0$

Exponent Rules and Logarithms:

#13. Write in simplest form: $3a^2 4b^{-4} a^6 b^4 c^3$

#14. Write in simplest form without using a fraction or negative exponents: $\frac{2e^{-3x}}{5e^{-7x}}$

#15. Simplify the logarithmic expression into one logarithm: $4 \log_3(x) + \log_3(y) - 3 \log_3(z) + \frac{1}{2} \log_3(x)$

#16. Expand the logarithmic expression to the sum and/or difference of factors of logarithms with no exponents.

$$\ln\left(\frac{5y^4}{x^6}\right)$$

Unit Circle Trigonometry and Basic Trig Identities:

#17. Evaluate (answer in exact form, no decimals): $\cos\left(\frac{-\pi}{3}\right) =$

#18. Evaluate (answer in exact form, no decimals): $\cot\left(\frac{7\pi}{6}\right) =$

#19. Evaluate (answer in exact form, no decimals): $\csc\left(\frac{5\pi}{3}\right) =$

#20. Evaluate (answer in exact form, no decimals): $\sin^{-1}\left(\frac{-\sqrt{3}}{2}\right) =$

#21. Evaluate (answer in exact form, no decimals): $\sin\left[\cos^{-1}\left(\frac{\sqrt{3}}{2}\right)\right] =$

#22. Simplify fully: $\frac{3\sin^3\theta}{\cos\theta} + 3\sin\theta\cos\theta$

Solving equations:

#23. Solve the equation (Exact answers only): $\frac{x^2 - 4}{3} = \frac{x}{4}$

#24. Solve the equation (Exact answers only): $4x^2 + x - 3 = 0$

#25. Solve the equation (Exact answers only): $e^{2x+6} = 4$

#26. Solve the equation (Exact answers only): $\ln(3x-1) = 5$

#27. Solve the equation (Exact answers only): $4\cos(\theta) - 2 = 0$ ($0 \leq \theta < 2\pi$)

#28. Solve the equation (Exact answers only): $2\sin^2(\theta) + 3\sin(\theta) - 2 = 0$ ($0 \leq \theta < 2\pi$)