## 2011 AP ${ }^{\circledR}$ CALCULUS BC FREE-RESPONSE QUESTIONS


4. The continuous function $f$ is defined on the interval $-4 \leq x \leq 3$. The graph of $f$ consists of two quarter circles and one line segment, as shown in the figure above. Let $g(x)=2 x+\int_{0}^{x} f(t) d t$.
(a) Find $g(-3)$. Find $g^{\prime}(x)$ and evaluate $g^{\prime}(-3)$.
(b) Determine the $x$-coordinate of the point at which $g$ has an absolute maximum on the interval $-4 \leq x \leq 3$. Justify your answer.
(c) Find all values of $x$ on the interval $-4<x<3$ for which the graph of $g$ has a point of inflection. Give a reason for your answer.
(d) Find the average rate of change of $f$ on the interval $-4 \leq x \leq 3$. There is no point $c,-4<c<3$, for which $f^{\prime}(c)$ is equal to that average rate of change. Explain why this statement does not contradict the Mean Value Theorem.

FRQ \#4c (NO Calculator) - Using graph of f and $\mathrm{f}^{\prime}$, evaluating integrals with geometry and by Fundamental Theorem of Calculus, $\mathrm{f}^{\prime}(\mathrm{x})$ applications, $\mathrm{f}^{\prime \prime}(\mathrm{x})$ applications

## 2018 AP ${ }^{\circledR}$ CALCULUS BC FREE-RESPONSE QUESTIONS



Graph of $g$
3. The graph of the continuous function $g$, the derivative of the function $f$, is shown above. The function $g$ is piecewise linear for $-5 \leq x<3$, and $g(x)=2(x-4)^{2}$ for $3 \leq x \leq 6$.
(a) If $f(1)=3$, what is the value of $f(-5)$ ?
(b) Evaluate $\int_{1}^{6} g(x) d x$.
(c) For $-5<x<6$, on what open intervals, if any, is the graph of $f$ both increasing and concave up? Give a reason for your answer.
(d) Find the $x$-coordinate of each point of inflection of the graph of $f$. Give a reason for your answer.

FRQ \#4d (NO Calculator) - Using graph of $f$ and $f^{\prime}$, evaluating integrals using geometry, $f^{\prime}(x)$ applications, $\mathrm{f}^{\prime \prime}(\mathrm{x})$ applications

# 2016 AP ${ }^{\oplus}$ CALCULUS BC FREE-RESPONSE QUESTIONS <br> CALCULUS BC <br> SECTION II, Part B <br> Time- $\mathbf{6 0}$ minutes <br> Number of problems-4 

## No calculator is allowed for these problems.


3. The figure above shows the graph of the piecewise-linear function $f$. For $-4 \leq x \leq 12$, the function $g$ is defined by $g(x)=\int_{2}^{x} f(t) d t$.
(a) Does $g$ have a relative minimum, a relative maximum, or neither at $x=10$ ? Justify your answer.
(b) Does the graph of $g$ have a point of inflection at $x=4$ ? Justify your answer.
(c) Find the absolute minimum value and the absolute maximum value of $g$ on the interval $-4 \leq x \leq 12$. Justify your answers.
(d) For $-4 \leq x \leq 12$, find all intervals for which $g(x) \leq 0$.

FRQ \#4e (NO Calculator) - Using graph of $f$ and $f^{\prime}$ derivatives (tangent lines), evaluating integrals with geometry, derivative rules, $\mathrm{f}^{\prime}(\mathrm{x})$ applications, $\mathrm{f}^{\prime \prime}(\mathrm{x})$ applications

## 2014 AP ${ }^{\oplus}$ CALCULUS BC FREE-RESPONSE QUESTIONS



Graph of $f$
3. The function $f$ is defined on the closed interval $[-5,4]$. The graph of $f$ consists of three line segments and is shown in the figure above. Let $g$ be the function defined by $g(x)=\int_{-3}^{x} f(t) d t$.
(a) Find $g(3)$.
(b) On what open intervals contained in $-5<x<4$ is the graph of $g$ both increasing and concave down? Give a reason for your answer.
(c) The function $h$ is defined by $h(x)=\frac{g(x)}{5 x}$. Find $h^{\prime}(3)$.
(d) The function $p$ is defined by $p(x)=f\left(x^{2}-x\right)$. Find the slope of the line tangent to the graph of $p$ at the point where $x=-1$.

## 2012 AP ${ }^{\circledR}$ CALCULUS BC FREE-RESPONSE QUESTIONS


3. Let $f$ be the continuous function defined on $[-4,3]$ whose graph, consisting of three line segments and a semicircle centered at the origin, is given above. Let $g$ be the function given by $g(x)=\int_{1}^{x} f(t) d t$.
(a) Find the values of $g(2)$ and $g(-2)$.
(b) For each of $g^{\prime}(-3)$ and $g^{\prime \prime}(-3)$, find the value or state that it does not exist.
(c) Find the $x$-coordinate of each point at which the graph of $g$ has a horizontal tangent line. For each of these points, determine whether $g$ has a relative minimum, relative maximum, or neither a minimum nor a maximum at the point. Justify your answers.
(d) For $-4<x<3$, find all values of $x$ for which the graph of $g$ has a point of inflection. Explain your reasoning.

